



**Faculty of Engineering and Technology**  
**Electrical and Computer Engineering Department**

**First Semester 2021/2022**

**Course 539: Special Topics:** Information Retrieval and Web Search

**Instructor:** Dr Adnan Yahya. **Midterm Exam**

**Time: 80 minutes max**

Please answer the following questions using the exam sheets only.

Question	Q1	Q2	Q3	Q4	Q5	Total
<b>ABET outcome</b>	e	a	e	a		
<b>Max grade</b>	21	20	21	20	21	103
<b>Earned</b>						

**Question 1 (21%):** Consider that our document collection S has the following 3 documents (after stop word removal): Work with English only except for item 3.

**D1: "large fast program"** برنامج سريع كبير

**D2: "large large fast train"** قطار سريع كبير كبير

**D3: "slow program"** برنامج بطيء

For all the documents, calculate the tf scores for all the terms in S. Order the terms in the vectors alphabetically. Compute idf values with no log and ignore normalization for terms and values. Given the following query:

**Q: "fast train program",** برنامج قطار سريع

1. 9%: Complete the following table for these documents and Query. Sort Terms alphabetically:

**Answer:**

Word	df	Idf= N/df=3/df	D1 tf↓ tf.idf	D2 tf↓ tf.idf	D3 tf↓ tf.idf	Q tf↓ tf.idf
W1 fast	2	3/2	1:3/2	1:3/2	0:0	1:3/2
W2 large	2	3/2	1:3/2	2:3	0:0	0:0
W3 program	2	3/2	1:3/2	0:0	1:3/2	1:3/2
W4 slow	1	3/1	0:0	0:0	1:3	0:0
W5 train	1	3/1	0:0	1:3	0:0	1:3

2. 9%: Rank D1, D2 and D3 with respect to the query Q according to the cosine metric and tf.idf. Explain why.

**Answer:**

$$|Q| = \sqrt{9/4 + 9/4 + 9} = \sqrt{27/2} = 3.67;$$

$$|D1| = \sqrt{9/4 + 9/4 + 9/4} = \sqrt{27/4} = 2.6$$

$$|D2| = \sqrt{9/4 + 9 + 9} = \sqrt{81/4} = 9/2 = 4.5$$

$$|D3| = \sqrt{9/4 + 9} = \sqrt{45/4} = 3.35$$

**Answer:**

$$\text{Sim}(Q, D1) / (|Q| * |D1|) = (9/4 + 9/4) / (3.67 * 2.6) = (9/2) / (3.67 * 2.6) = 0.47 \text{-----} (\text{Rank:2})$$

$$\text{Sim}(Q, D2) / (|Q| * |D2|) = (9/4 + 9) / (3.67 * 4.5) = 11.25 / 3.67 * 4.5 = 0.68 \text{-----} (\text{Rank:1})$$

$$\text{Sim}(Q, D3) / (|Q| * |D3|) = (9/4) / (3.67 * 3.35) = 4.5 / 3.67 * 1.5 = 0.18 \text{-----} (\text{Rank:3})$$

3. 3% Give three possible words to extend the query برنامج قطار سريع for better recall.

**Example:** جدول ترين اكبرس [example: many others possible: add terms at small distance from any of the words of the query, from synsets, ....]

**Question 2 (20%):**

a. A search engine has a collection of 7,000,000 documents with 700 words per document, on average.

(i) 3% What is the minimal length for document IDs for the postings? In bits and in full bytes. Why?

**Answer:**

$2^{22} < 7,000,000 < 2^{23}$  so we need **23 bits and 3 bytes**.

**Document length is irrelevant here!**

(ii) 3% If the vocabulary size is 300,000 terms and the average dictionary word length is 10 characters. How many **bits** do you need for pointers if one is to store the dictionary as a single string with pointers to the start of each **word** (what is the length of each pointer). In bits and in full bytes. Why?

**Answer:** 300,000 terms of 10 character/bytes on average: 3,000,000. Each pointer points to one of these 3,000,000 characters and for that we need **22 bits and 3 bytes**.

(iii) 3% Compute the  $\gamma$ -code and the variable byte code for the decimal number 514. Explain.

**Answer:**  $\gamma$ -code:  $514 = 512 + 2 = 100000000 + 10 = 100000010$  Offset = **00000010** of length 0 so the  $\gamma$ -code is **11111111000000010**

variable byte code: **10000000**    **00000101** [rightmost bit is continuation if 0, stop if 1] Can be reverse.

(iv) 4% Recover the gap values (in decimal) for the following string representing  $\gamma$ -encoding of a sequence of gaps in a posting list.

111110101001110111111101010101

**Answer:**

**1111101010011101111111010101**  
**110100    1111    11010 11**  
**52        15        26 3**

(v) 3% Consider a letter bigram index for wildcard queries. Give an example of a string that falsely matches the wildcard query **mon\*hs** if search is simply using a conjunction (ANDing) of bigrams.

**Answer:** -m, mo, on, + hs, s- → **moremonths**

**Has all the bigrams but is not correct.**

(vi) 4% Represent the binary number 10101011101010110 as a variable length code with a continuation bit.

**Answer:**

**10101011101010110** → divide into 7 bits and add continuation/end bits → **101010111101010100001100**  
**1** means continue, **0** means end. [other options possible]

**Question 3 (21%):**

1. 10% Shown below is a portion of a positional index in the format:

**term:** doc1: <position1, position2, . . . >; doc2: <position1, position2, . . . >; etc.

**angels:** 2: <36,174,252,651>; 4: <12,22,102,432>; 7: <17>;  
**fools:** 2: <1,17,74,222>; 4: <8,78,108,458>; 7: <3,13,23,193>;  
**fear:** 2: <87,704,722,901>; 4: <13,43,113,433>; 7: <18,328,528>;  
**in:** 2: <3,37,76,444,851>; 4: <10,20,110,470,500>; 7: <5,15,25,195>;  
**rush:** 2: <2,66,194,321,702>; 4: <9,69,149,429,569>; 7: <4,14,404>;  
**to:** 2: <47,86,234,999>; 4: <14,24,774,944>; 7: <199,319,599,709>;  
**tread:** 2: <57,94,333>; 4: <15,35,155>; 7: <20,320>;  
**where:** 2: <67,124,393,1001>; 4: <11,41,101,421,431>; 7: <16,36,736>;

Which document(s) if any match each of the following queries, where each expression within quotes is a phrase query?

-3% “fools rush in” –**Order important: phrase queries- Answer: {D2, D4, D7}**

- 3% “fools rush in” AND “angels fear to tread” **Answer: {D2, D4, D7} ∩ {D4}={D4}**  
**{D2, D4, D7} {D4}**

-2% List the last known 4 words of document 7: **Answer:**

**fear[528]→to[599]→ to[709]→ where[736] (order important, numbers not)**

-2% If  $|s_i|$  denotes the length of string  $s_i$ , show that the edit distance between  $s_1$  and  $s_2$  is never more than  $\max(|s_1|, |s_2|)$ .

**Answer: we can always replace the characters of the shorter by those of the longer then add the rest.**

**Or we can always replace the characters of the longer by those of the shorter then delete the rest. In both cases we have the max as the limit.**

2. Select the **BEST** Match: 11%

?	Text		Defines
<b>P</b>	The vocabulary size of a text can be estimated using	A	Similarity Measure
<b>F</b>	A metric used to measure the importance of a term in a text document collection	B	Distance Measure
<b>I</b>	# of changes needed to convert one string into another	C	Tokenization
<b>D</b>	Levenshtein distance:	D	Insert-Delete-replace one step
<b>L</b>	Damerau-Levenshtein Distance	E	Insert-Exchange 1 step
<b>K</b>	Removing most frequent words in the collection	F	IDF
<b>J</b>	Removing least frequent words in the collection	G	TF
<b>C</b>	Dividing a string into words	H	Normalization
<b>A</b>	A measure of how close documents are to each other	I	Levenshtein Distance
<b>M</b>	Removing word affixes: suffixes and prefixes	J	Typo (error) Cleaning
<b>N</b>	Number of non-positional postings for a term	K	Stop word removal
		L	Insert-Delete-replace-exchange 1 step
		M	Stemming
		N	DF
		O	Zipf 's Law
		P	Heap's Law

		Q	Recall
		R	Inverted Index

**Question 4 (20%)**

- 1- 4% Assuming Zipf's law with a corpus independent constant  $A = 0.1$ , what is the fewest number of most common words that together account for more than 19% of word occurrences (i.e. the minimum value of  $m$  such that at least 17% of word occurrences are one of them most common words).

**PR=0.1 → P=0.1/R: Top 3 words:  $0.1/1 + 0.1/2 + 0.1/3 = 0.1 + 0.05 + 0.033 \rightarrow 18.3%$  Top 4 words:  $0.1/1 + 0.1/2 + 0.1/3 + 0.1/4 = 0.1 + 0.05 + 0.033 + 0.025 \rightarrow 20.8%$  So the min number is 4**

- 2- 4% Assume the 4<sup>th</sup> most frequent word has frequency 16000. Can you estimate the number of distinct words (types) in the dictionary? Explain

**PR = 0.1 → at rank 4:  $P = 16000/N$ ;  $(16000/N) * 4 = 0.1 \rightarrow N = 640,000$  (total number of Tokens).**

**Assume the highest ranking term (at rank D where D is the number of types) occurs only once (reasonable assumption for this size):  $(1/N) * D = 0.1 \rightarrow D = 0.1 * N = 64,000$ : this is the number of types.**

- 3- 3% Assume the 4<sup>th</sup> most frequent word has frequency 1600. Can you estimate the frequency of the most frequent word in the dictionary? Explain.

**$F_4 = F_1/4$ ;  $F_1 = F_4 * 4 = 6400$**

- 4- If we add another collection to this one with similar characteristics: exactly the same **number** of words and the same **vocabulary size** (but no duplicate documents): In your opinion:

4-1. 3% What will happen to the new vocabulary size?

**By Heap's law the dictionary size should increase: though not double!**

4-2. 3% What will happen to the frequency of the 10 most frequent words? Will they change? Remain the same? Explain.

**Yes. The frequencies are most likely to increase as they are generally stop words frequent in most documents. Relative frequency need not change, though**

- 5- 3% Prove that text power laws have a linear log-log graph.

**Power laws have the form (X,Y: variables; K,Z are constants):  $Y = K * X^Z \rightarrow \log Y = \log K + Z * \log X = K_1 + K_2 * \log X$**

**Linear in terms of logX, LogY.**

